

Identify the vertex, axis of symmetry, min/max value, y-intercept, and x-intercepts of each. Then sketch the graph. Label the x-intercept(s), y-intercept, vertex, and axis of symmetry on each graph.

y-intercept: (0, 12)

\*Not shown because it is above the highest value on the graph.

1)  $y = x^2 + 8x + 12$

$$f(x) = (x^2 + 8x + 16) + 12 - 16$$

$$\left(\frac{8}{2}\right)^2 = (4)^2 = 16$$

$$f(x) = (x^2 + 8x + 16) + 12 - 16$$

$$f(x) = (x + 4)^2 - 4$$

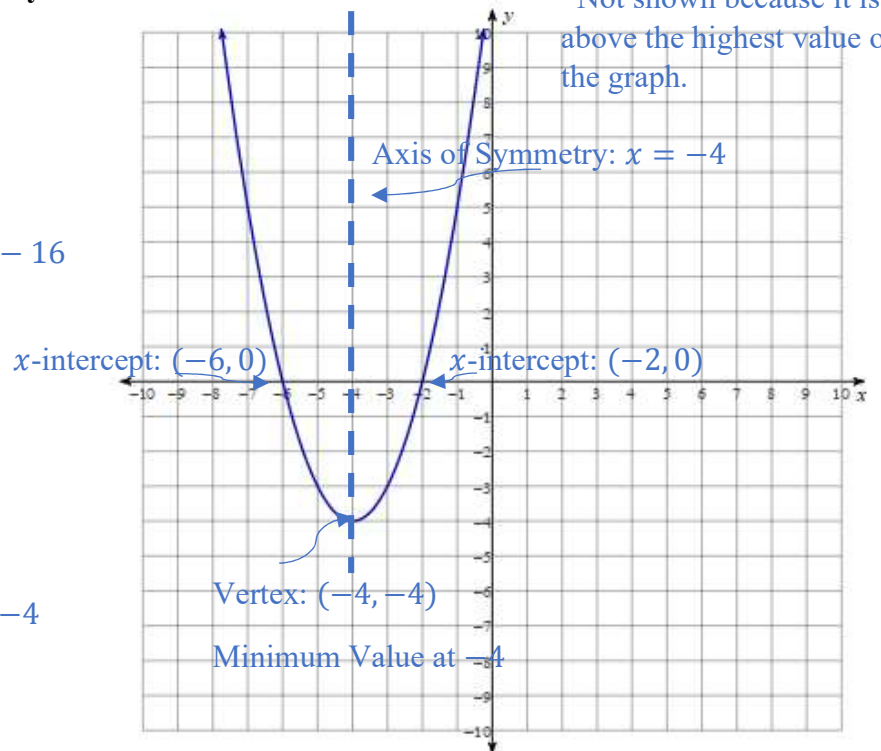
Vertex: (-4, -4)

Axis of Symmetry:  $x = -4$

Min/Max Value: Minimum = -4

y-intercept: (0, 12)

x-intercept(s): (-6, 0) & (-2, 0)



2)  $y = -x^2 - 4x$

$$f(x) = -(x^2 + 4x + 4) + 4$$

$$\left(\frac{4}{2}\right)^2 = (2)^2 = 4$$

$$f(x) = -(x^2 + 4x + 4) + 4$$

$$f(x) = -(x + 2)^2 + 4$$

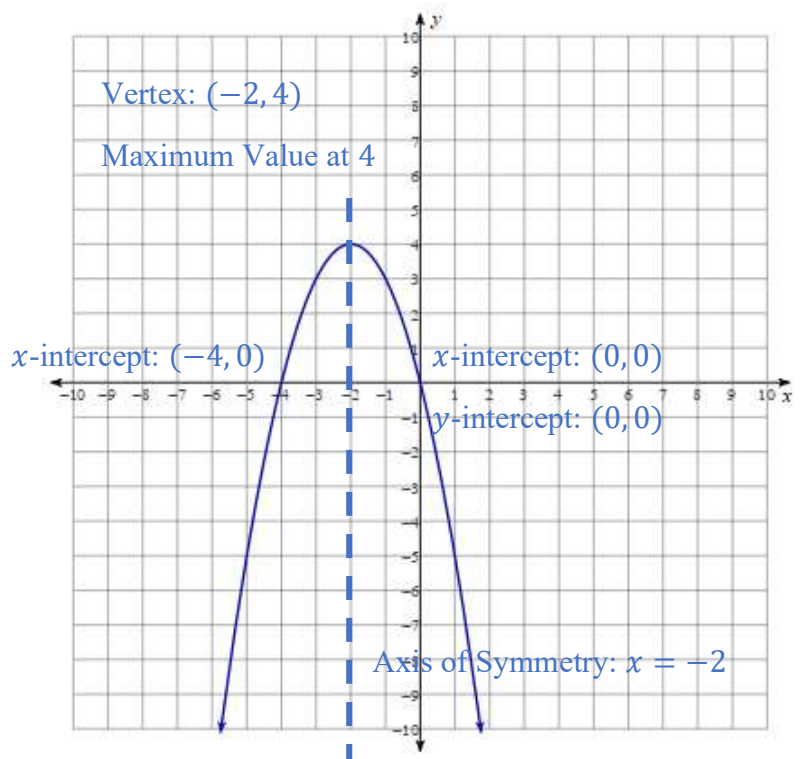
Vertex: (-2, 4)

Axis of Symmetry:  $x = -2$

Min/Max Value: Maximum = 4

y-intercept: (0, 0)

x-intercept(s): (-4, 0) & (0, 0)



3)  $y = -2x^2 + 20x - 51$

$$f(x) = -2(x^2 - 10x \quad ) - 51$$

$$\left(\frac{-10}{2}\right)^2 = (-5)^2 = 25$$

$$f(x) = -2(x^2 - 10x + 25) - 51 + 50$$

$$f(x) = -2(x - 5)^2 - 1$$

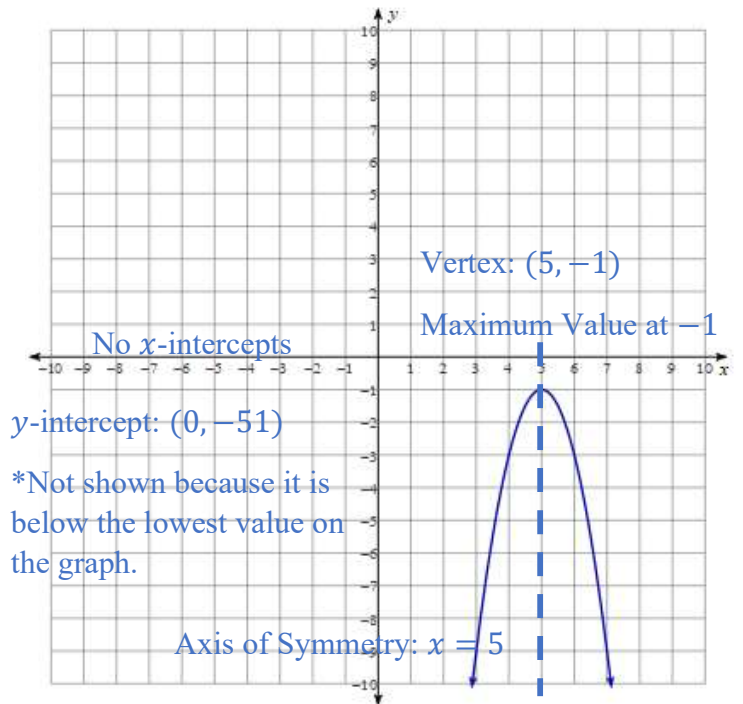
Vertex:  $(5, -1)$

Axis of Symmetry:  $x = 5$

Min/Max Value: Maximum =  $-1$

y-intercept:  $(0, -51)$

x-intercept(s): None



4)  $y = x^2 + 12x + 36$

$$f(x) = (x^2 + 12x \quad ) + 36$$

$$\left(\frac{12}{2}\right)^2 = (6)^2 = 36$$

$$f(x) = (x^2 + 12x + 36) + 36 - 36$$

$$f(x) = (x + 6)^2$$

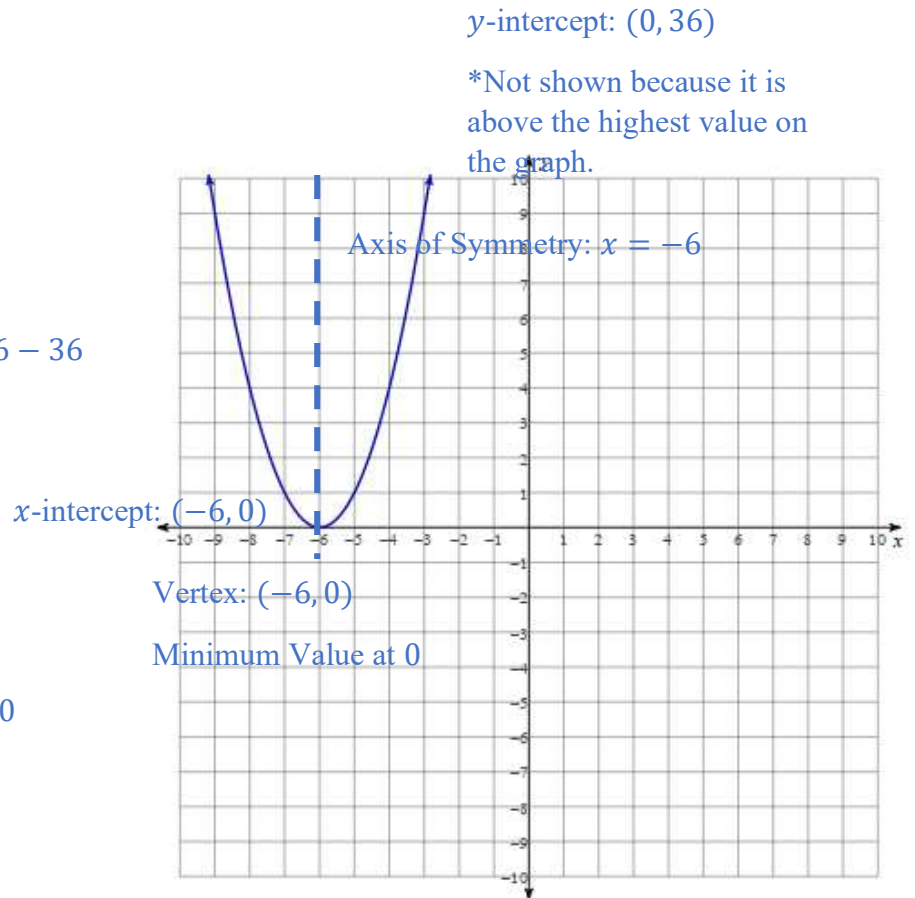
Vertex:  $(-6, 0)$

Axis of Symmetry:  $x = -6$

Min/Max Value: Minimum =  $0$

y-intercept:  $(0, 36)$

x-intercept(s):  $(-6, 0)$



5)  $y = -x^2 + 4x - 3$

$$f(x) = -(x^2 - 4x \quad ) - 3$$

$$\left(\frac{-4}{2}\right)^2 = (-2)^2 = 4$$

$$f(x) = -(x^2 - 4x + 4) - 3 + 4$$

$$f(x) = -(x - 2)^2 + 1$$

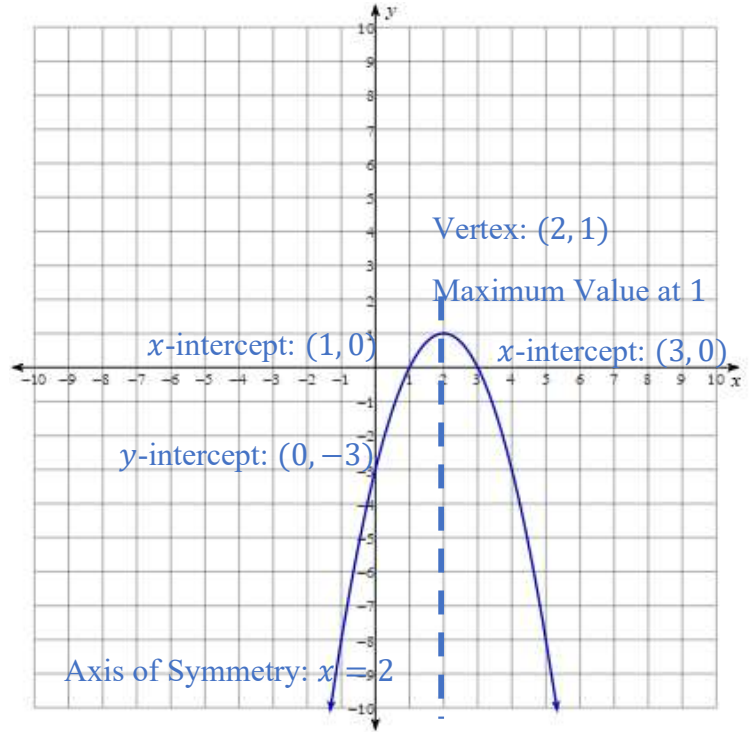
Vertex:  $(2, 1)$

Axis of Symmetry:  $x = 2$

Min/Max Value: Maximum = 1

y-intercept:  $(0, -3)$

x-intercept(s):  $(1, 0)$  &  $(3, 0)$



6)  $y = -2x^2 - 4x - 3$

$$f(x) = -2(x^2 + 2x \quad ) - 3$$

$$\left(\frac{2}{2}\right)^2 = (1)^2 = 1$$

$$f(x) = -2(x^2 + 2x + 1) - 3 + 2$$

$$f(x) = -2(x + 1)^2 - 1$$

Vertex:  $(-1, -1)$

Axis of Symmetry:  $x = -1$

Min/Max Value: Maximum = -1

y-intercept:  $(0, -3)$

x-intercept(s): None

