

## Lesson 1.8 Notes

| $x$ | $y$ | Describe the pattern.  | Recursive rule:                           | Explicit rule:         | Arithmetic, Geometric, or Neither? |
|-----|-----|--|---|------------------------|------------------------------------|
| 1   | 5   | Each term is twice as much as the term before it. So, we are multiplying by two. | $f(0) = 2.5$<br>$f(x) = f(x - 1) \cdot 2$ | $f(x) = 2^x \cdot 2.5$ | Geometric                          |
| 2   | 10  |  |   |                        |                                    |
| 3   | 20  |  |   |                        |                                    |
| 4   | 40  |  |   |                        |                                    |
| 5   | ?   |  |   |                        |                                    |
| ... | ... |  |   |                        |                                    |
| $n$ | ?   |  |   |                        |                                    |

| $x$ | $y$ | Describe the pattern.   | Recursive rule:                     | Explicit rule:   | Arithmetic, Geometric, or Neither? |
|-----|-----|---|-------------------------------------|------------------|------------------------------------|
| 1   | -8  | Each term is 9 less than the previous term. So, we are subtracting 9. | $f(0) = 1$<br>$f(x) = f(x - 1) - 9$ | $f(x) = -9x + 1$ | Arithmetic                         |
| 2   | -17 |   |                                     |                  |                                    |
| 3   | -26 |   |                                     |                  |                                    |
| 4   | -35 |   |                                     |                  |                                    |
| 5   | -44 |   |                                     |                  |                                    |
| 6   | -53 |   |                                     |                  |                                    |
| ... | ... |   |                                     |                  |                                    |
| $n$ | ?   |   |                                     |                  |                                    |

| $x$ | $y$ | Describe the pattern.  | Recursive rule:                                   | Explicit rule:                 | Arithmetic, Geometric, or Neither? |
|-----|-----|--|---|--------------------------------|------------------------------------|
| 1   | 2   | Each term is three times as much as the term before it. So, we are multiplying by three. | $f(0) = \frac{2}{3}$<br>$f(x) = f(x - 1) \cdot 3$ | $f(x) = 3^x \cdot \frac{2}{3}$ | Geometric                          |
| 2   | 6   |  |   |                                |                                    |
| 3   | 18  |  |   |                                |                                    |
| 4   | 54  |  |   |                                |                                    |
| 5   | 162 |  |   |                                |                                    |
| 6   | 486 |  |   |                                |                                    |
| ... | ... |  |   |                                |                                    |
| $n$ | ?   |  |   |                                |                                    |

| $x$ | $y$ | Describe the pattern.  | Recursive rule:                       | Explicit rule:   | Arithmetic, Geometric, or Neither? |
|-----|-----|--|---------------------------------------|------------------|------------------------------------|
| 1   | 3   | Each term is 12 more than the previous term. So, we are adding 12. | $f(0) = -9$<br>$f(x) = f(x - 1) + 12$ | $f(x) = 12x - 9$ | Arithmetic                         |
| 2   | 15  |  |                                       |                  |                                    |
| 3   | 27  |  |                                       |                  |                                    |
| 4   | 39  |  |                                       |                  |                                    |
| 5   | 51  |  |                                       |                  |                                    |
| 6   | ?   |  |                                       |                  |                                    |
| ... | ... |  |                                       |                  |                                    |
| $n$ | ?   |  |                                       |                  |                                    |

| $x$ | $y$            |
|-----|----------------|
| 0   | 1              |
| 1   | $1\frac{3}{5}$ |
| 2   | $2\frac{1}{5}$ |
| 3   | $2\frac{4}{5}$ |
| 4   | $3\frac{2}{5}$ |
| 5   | 4              |
| ... | ...            |
| $n$ | ?              |

| Describe the pattern.   | Recursive rule:                            | Explicit rule:            | Arithmetic, Geometric, or Neither? |
|---|--|---------------------------|------------------------------------|
| Each term is $\frac{3}{5}$ more than the previous term.** So, we are adding $\frac{3}{5}$ . | $f(0) = 1$ $f(x) = f(x - 1) + \frac{3}{5}$ | $f(x) = \frac{3}{5}x + 1$ | Arithmetic                         |

\*\*If you change all of the y-values to improper fractions with denominators of 5 it becomes more clear:  $\frac{5}{5}, \frac{8}{5}, \frac{11}{5}, \frac{14}{5}, \frac{17}{5}, \frac{20}{5}, \dots$

| $x$ | $y$             |
|-----|-----------------|
| 1   | 10              |
| 2   | 2               |
| 3   | $\frac{2}{5}$   |
| 4   | $\frac{2}{25}$  |
| 5   | $\frac{2}{125}$ |
| 6   | $\frac{2}{625}$ |
| ... | ...             |
| $n$ | ?               |

| Describe the pattern.  | Recursive rule:                                 | Explicit rule:                               | Arithmetic, Geometric, or Neither? |
|--|---|--|------------------------------------|
| Each term is being divided by 5. So, we are multiplying by $\frac{1}{5}$ . | $f(0) = 50$ $f(x) = f(x - 1) \cdot \frac{1}{5}$ | $f(x) = \left(\frac{1}{5}\right)^x \cdot 50$ | Geometric                          |

| $x$ | $y$     |
|-----|---------|
| 1   | -1      |
| 2   | 0.2     |
| 3   | -0.04   |
| 4   | 0.008   |
| 5   | -0.0016 |
| 6   | 0.00032 |
| ... | ...     |
| $n$ | ?       |

| Describe the pattern.  | Recursive rule:                           | Explicit rule:            | Arithmetic, Geometric, or Neither? |
|--|---|---------------------------|------------------------------------|
| Each term is being multiplied by 0.2.* Since the sign is alternating from positive to negative we are multiplying by -0.2. | $f(0) = 5$ $f(x) = f(x - 1) \cdot (-0.2)$ | $f(x) = (-0.2)^x \cdot 5$ | Geometric                          |

\*Since the decimals are adding one zero in front of the number, I know it is multiplying by 0.2, not 2.

| $x$ | $y$ |
|-----|-----|
| 0   | 3   |
| 1   | 4   |
| 2   | 7   |
| 3   | 12  |
| 4   | 19  |
| 5   | ?   |
| ... | ... |
| $n$ | ?   |

| Describe the pattern.                    | Recursive rule:                       | Explicit rule:   | Arithmetic, Geometric, or Neither? |
|--|---------------------------------------|------------------|------------------------------------|
| Each term adds an increasing odd number. | $f(0) = 3$ $f(x) = f(x - 1) + 2x - 1$ | $f(x) = x^2 + 3$ | Neither                            |

\*\*\*I do not expect you to be able to write the recursive and explicit rule for a function that is "neither".

**Other important notes from today:**

Find the constant ratio for each geometric sequence.

- 1) 16, 24, 36, ...  $\frac{36}{24} = 1.5, \frac{24}{16} = 1.5$  The constant ratio is 1.5.
- 2)  $\frac{5}{2}, \frac{5}{3}, \frac{10}{9}, \dots$   $\frac{10}{9} \div \frac{5}{3} = 1.5, \frac{5}{3} \div \frac{5}{2} = 1.5$  The constant ratio is 1.5.
- 3) 81, 108, 144, ...  $\frac{144}{108} = \frac{4}{3}, \frac{108}{81} = \frac{4}{3}$  The constant ratio is  $\frac{4}{3}$ .

Fill in the blanks for each table, then write the recursive and explicit equation for each sequence.

1) .

| x | y     |
|---|-------|
| 1 | 4     |
| 2 | 16    |
| 3 | 64    |
| 4 | 256   |
| 5 | 1,024 |

Recursive:  
 $f(0) = 1$   
 $f(x) = f(x - 1) \cdot 4$

Explicit:  
 $f(x) = 4^x$

2) .

| x | y  |
|---|----|
| 1 | 3  |
| 2 | 5  |
| 3 | 7  |
| 4 | 9  |
| 5 | 11 |

Recursive:  
 $f(0) = 1$   
 $f(x) = f(x - 1) + 2$

Explicit:  
 $f(x) = 2x + 1$

3) .

| x | y              |
|---|----------------|
| 1 | -64            |
| 2 | -16            |
| 3 | -4             |
| 4 | -1             |
| 5 | $-\frac{1}{4}$ |

Recursive:  
 $f(0) = -256$   
 $f(x) = f(x - 1) \cdot \frac{1}{4}$

Explicit:  
 $f(x) = \left(\frac{1}{4}\right)^x \cdot (-256)$

Write each equation of the line in  $y = mx + b$  form.

