

## Writing Equations in Slope-Intercept Form Given Two Points

\*\*Remember that slope-intercept form is  $y = mx + b$  where  $m$  is slope and  $b$  is the  $y$ -intercept.

### Example 1: Write an Equation Given Two Points

Write an equation of a line that passes through  $(-3, -1)$  and  $(6, -4)$

The first thing we have to do when given two points is calculate slope.

$x$	$y$
-3	-1
6	-4

+9      -3

$$\frac{\Delta y}{\Delta x} = \frac{-3}{9} = -\frac{1}{3}$$

The slope ( $m$ ) is  $-\frac{1}{3}$ .

$$y = mx + b$$

We can replace  $m$  with the slope we just calculated.

$$y = -\frac{1}{3}x + b$$

We can choose to use either of the two points: ***\*\*You do not need to plug both in. You pick one and use that one. I'm using both to show that it doesn't matter which you choose.***

If we use  $(-3, -1)$ :

Replace  $x$  with  $-3$ .

Replace  $y$  with  $-1$ .

$$-1 = -\frac{1}{3}(-3) + b$$

Multiply the  $-\frac{1}{3} \cdot -3$ .

$$-1 = 1 + b$$

Solve for  $b$ :

$$-1 = 1 + b$$

$$-1 - 1$$

$$-2 = b$$

If we use  $(6, -4)$ :

Replace  $x$  with  $6$ .

Replace  $y$  with  $-4$ .

$$-4 = -\frac{1}{3}(6) + b$$

Multiply the  $-\frac{1}{3} \cdot 6$ .

$$-4 = -2 + b$$

Solve for  $b$ :

$$-4 = -2 + b$$

$$+2 \quad +2$$

$$-2 = b$$

Notice that we get the same y-intercept regardless of which point we choose to plug in for x and y.

Our final answer is when we write the equation of the line with both the slope and y-intercept replaced.

$$y = -\frac{1}{3}x - 2 \quad \text{**This is our solution}$$

### Example 2: Write an Equation Given Two Points

Write an equation of a line that passes through (5, 1) and (8, -2)

The first thing we have to do when given two points is calculate slope.

x	y
5	1
8	-2

+3      -3

$$\frac{\Delta y}{\Delta x} = \frac{-3}{3} = -1$$

The slope (m) is  $-1$ .

$$y = mx + b$$

We can replace m with the slope we just calculated.

$$y = -1x + b$$

We can choose to use either of the two points: ***\*\*You do not need to plug both in. You pick one and use that one. I'm using both to show that it doesn't matter which you choose.***

If we use (5, 1):

Replace x with 5.

Replace y with 1.

$$1 = -1(5) + b$$

Multiply the  $-1 \cdot 5$ .

$$1 = -5 + b$$

If we use (8, -2):

Replace x with 8.

Replace y with -2.

$$-2 = -1(8) + b$$

Multiply the  $-1 \cdot 8$ .

$$-2 = -8 + b$$

Solve for b:

$$1 = -5 + b$$

$$+5 \quad +5$$

$$6 = b$$

Solve for b:

$$-2 = -8 + b$$

$$+8 \quad +8$$

$$6 = b$$

Notice that we get the same y-intercept regardless of which point we choose to plug in for x and y.

Our final answer is when we write the equation of the line with both the slope and y-intercept replaced.

$$y = -1x + 6 \quad \text{** A } -1x \text{ is the same as } -x$$

$$y = -x + 6 \quad \text{**This is our solution}$$

### Example 3: Write an Equation Given Two Points

Write an equation of a line that passes through (6, 0) and (0, 4)

The first thing we have to do when given two points is calculate slope.

	$x$	$y$	
	6	0	
-6	0	4	+4

$$\frac{\Delta y}{\Delta x} = \frac{4}{-6} = -\frac{2}{3}$$

The slope (m) is  $-\frac{2}{3}$ .

$$y = mx + b$$

We can replace m with the slope we just calculated.

$$y = -\frac{2}{3}x + b$$

We can choose to use either of the two points: **\*\*You do not need to plug both in. You pick one and use that one. I'm using both to show that it doesn't matter which you choose.**

If we use (6, 0):

Replace x with 6.

Replace y with 0.

If we use (0, 4):

Replace x with 0.

Replace y with 4.

$$0 = -\frac{2}{3}(6) + b$$

Multiply the  $-\frac{2}{3} \cdot 6$ .

$$0 = -4 + b$$

Solve for b:

$$0 = -4 + b$$

$$+4 \quad +4$$

$$4 = b$$

$$4 = -\frac{2}{3}(0) + b$$

Multiply the  $-\frac{2}{3} \cdot 0$ .

$$4 = 0 + b$$

Solve for b:

$$4 = 0 + b$$

$$4 = b$$

Notice that we get the same y-intercept regardless of which point we choose to plug in for x and y.

Our final answer is when we write the equation of the line with both the slope and y-intercept replaced.



$$y = -\frac{2}{3}x + 4 \quad \text{**This is our solution}$$

#### Example 4: Write an Equation Given Two Points

Write an equation of a line that passes through (5, 2) and (-7, -4)

The first thing we have to do when given two points is calculate slope.

x	y
5	2
-7	-4

$-12$    $-6$  

$$\frac{\Delta y}{\Delta x} = \frac{-6}{-12} = \frac{1}{2}$$

The slope (m) is  $\frac{1}{2}$ .

$$y = mx + b$$

We can replace m with the slope we just calculated.

$$y = \frac{1}{2}x + b$$

We can choose to use either of the two points: **\*\*You do not need to plug both in. You pick one and use that one. I'm using both to show that it doesn't matter which you choose.**

If we use (5, 2):

Replace x with 5.

Replace y with 2.

$$2 = \frac{1}{2}(5) + b$$

Multiply the  $\frac{1}{2} \cdot 5$ .

$$2 = 2\frac{1}{2} + b$$

Solve for b:

$$2 = 2\frac{1}{2} + b$$

$$-2\frac{1}{2} \quad -2\frac{1}{2}$$

$$-\frac{1}{2} = b$$

If we use (-7, -4):

Replace x with -7.

Replace y with -4.

$$-4 = \frac{1}{2}(-7) + b$$

Multiply the  $\frac{1}{2} \cdot -7$ .

$$-4 = -3\frac{1}{2} + b$$

Solve for b:

$$-4 = -3\frac{1}{2} + b$$

$$+3\frac{1}{2} \quad +3\frac{1}{2}$$

$$-\frac{1}{2} = b$$

Notice that we get the same y-intercept regardless of which point we choose to plug in for x and y.

Our final answer is when we write the equation of the line with both the slope and y-intercept replaced.

$$y = \frac{1}{2}x - \frac{1}{2} \quad \text{**This is our solution}$$

### Example 5: Write an Equation Given Two Points

Write an equation of a line that passes through (2, -3) and (8, -3)

The first thing we have to do when given two points is calculate slope.

x	y
2	-3
8	-3

+6      +0

$$\frac{\Delta y}{\Delta x} = \frac{0}{6} = 0$$

The slope (m) is 0.

Slopes of zero define horizontal lines whose equations are of the form  $y = \#$

In both of the points  $(2, -3)$  and  $(8, -3)$ ,  $-3$  is the  $y$ -value. So, our equation must be:

$$y = -3$$

### Example 6: Write an Equation Given Two Points

Write an equation of a line that passes through  $(6, -1)$  and  $(6, 2)$

The first thing we have to do when given two points is calculate slope.

$x$	$y$
6	-1
6	2

+0      +3

$$\frac{\Delta y}{\Delta x} = \frac{3}{0} = \text{undefined}$$

The slope ( $m$ ) is undefined.

Undefined slopes are vertical lines whose equations are  $x = \#$ .

In both of the points  $(6, -1)$  and  $(6, 2)$ ,  $6$  is the  $x$ -value. So, our equation must be:

$$x = 6$$