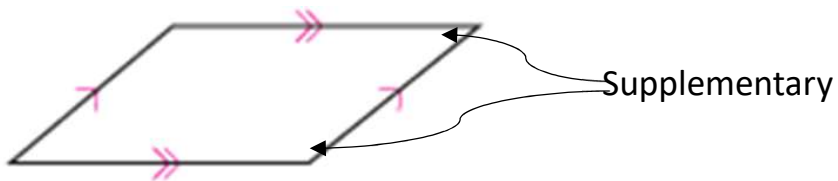


Lesson 5.5 – Properties of Parallelograms

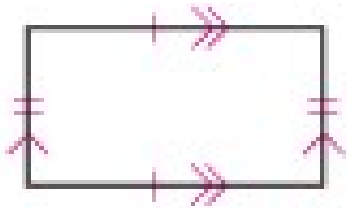
Parallelogram Opposite Angles Conjecture - The opposite angles of a parallelogram are congruent.



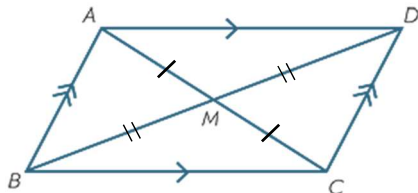
Parallelogram Consecutive Angles Conjecture - The consecutive angles of a parallelogram are supplementary.



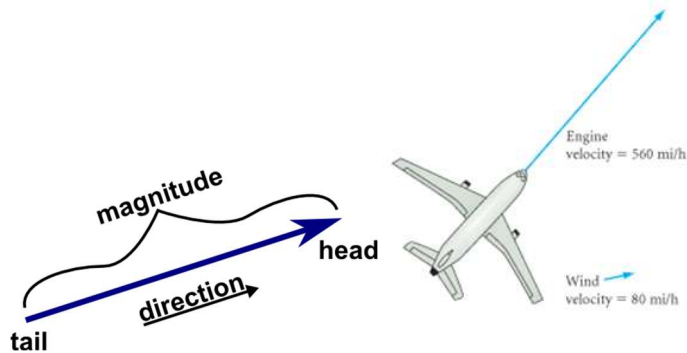
Parallelogram Opposite Sides Conjecture - The opposite sides of a parallelogram are congruent.



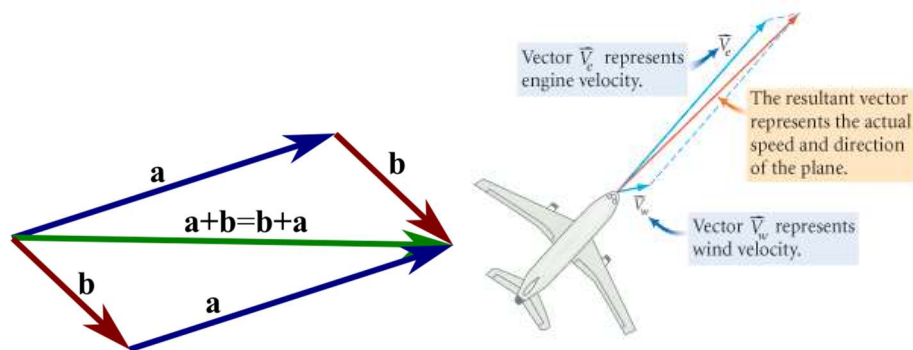
Parallelogram Diagonals Conjecture - The diagonals of a parallelogram bisect each other.



Vector - A vector is a quantity that has both magnitude and direction.

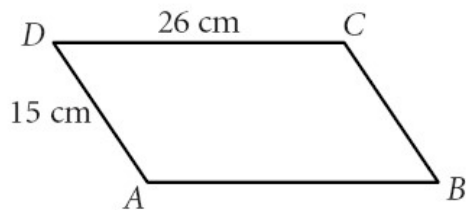


Resultant Vector - A resultant vector is the sum of vectors. It can be found by drawing the diagonal of the parallelogram with the vectors as sides.



Example 1: Find the missing measures in the parallelogram.

Perimeter $ABCD =$ _____



We know that the opposite sides of a parallelogram are congruent. That means that $AB = 26$ cm and $CB = 15$ cm. To find the perimeter, we can add all four sides.

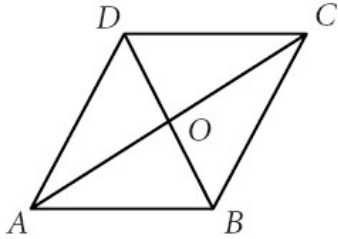
$$15 + 26 + 15 + 26 = 82$$

Perimeter $ABCD = 82$ cm

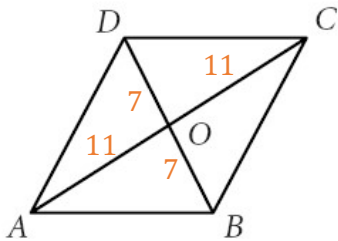
Example 2: Find the missing measures in the parallelogram.

$AO = 11$, and $BO = 7$

$AC = \underline{\hspace{2cm}}$, $BD = \underline{\hspace{2cm}}$



We know that the diagonals of a parallelogram bisect each other. So, $AO = OC$ and $BO = OD$.



To find AC , we need to add AO and OC .

$$11 + 11 = 22$$

$$\mathbf{AC = 22}$$

To find BD , we need to add BO and OD .

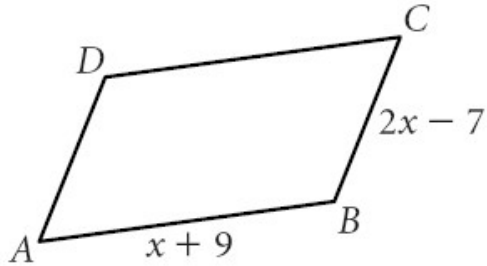
$$7 + 7 = 14$$

$$\mathbf{BD = 14}$$

Example 3: Find the missing measures in the parallelogram.

Perimeter $ABCD = 46$

$AB = \underline{\hspace{2cm}}$, $BC = \underline{\hspace{2cm}}$



We know that opposite sides of a parallelogram are congruent. So, this parallelogram has two sides with length $x + 9$ and two sides with length $2x - 7$. If we add up all four sides, we should get the perimeter of 46.

$$2(x + 9) + 2(2x - 7) = 46$$

$$2x + 18 + 4x - 14 = 46$$

$$6x + 4 = 46$$

$$\begin{array}{r} -4 \quad -4 \\ 6x + 4 = 46 \\ \hline 6x = 42 \end{array}$$

$$6x = 42$$

$$\begin{array}{r} \overline{6} \quad \overline{6} \\ 6x = 42 \\ \hline x = 7 \end{array}$$

$$x = 7$$

$$AB = x + 9 = 7 + 9 = 16$$

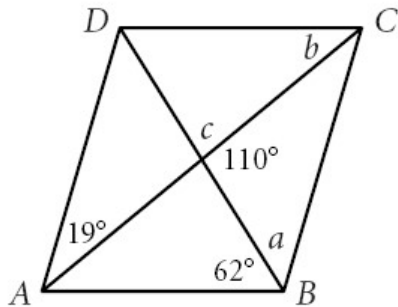
$$\mathbf{AB = 16}$$

$$BC = 2x - 7 = 2(7) - 7 = 14 - 7 = 7$$

$$\mathbf{BC = 7}$$

Example 4: Find the missing measures in the parallelogram.

$a = \underline{\hspace{2cm}}$, $b = \underline{\hspace{2cm}}$, $c = \underline{\hspace{2cm}}$

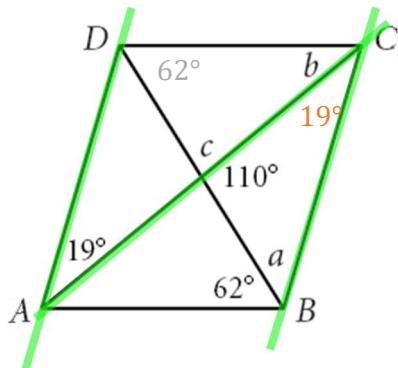
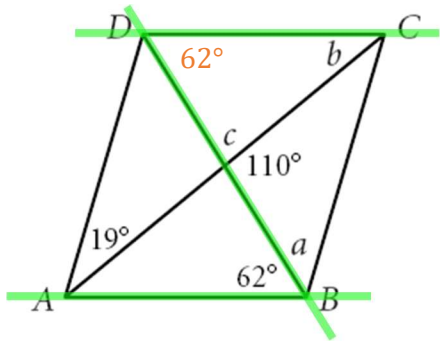


We can start by finding c since we know it is a linear pair with the 110° angle.

$$180 - 110 = 70$$

$$c = 70^\circ$$

Since this is a parallelogram, we can find the measures of alternate interior angles to those we know.



We can find a using the triangle with a , 110° , and 19° .

$$110 + 19 = 129$$

$$180 - 129 = 51$$

$$a = 51^\circ$$

We can find b using the triangle with b , c , and 62° .

$$70 + 62 = 132$$

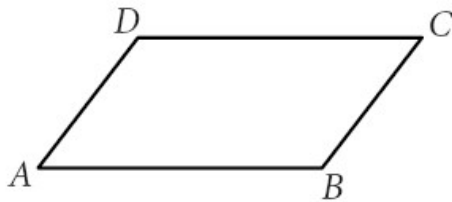
$$180 - 132 = 48$$

$$b = 48^\circ$$

Example 5: Find the missing measures in the parallelogram.

Perimeter $ABCD = 119$, and $BC = 24$

$$AB = \underline{\hspace{2cm}}$$



We know that opposite sides of a parallelogram are congruent. Since $BC = 24$ then $AD = 24$. We do not know the length of AB or DC , but we know they will be the same. So, let's use x to represent their measures. Adding all of the sides will give us the perimeter of 119.

$$2(24) + 2(x) = 119$$

$$48 + 2x = 119$$

$$\begin{array}{r} -48 \end{array} \quad \begin{array}{r} -48 \end{array}$$

$$2x = 71$$

$$\frac{\bar{}}{2} \quad \frac{\bar{}}{2}$$

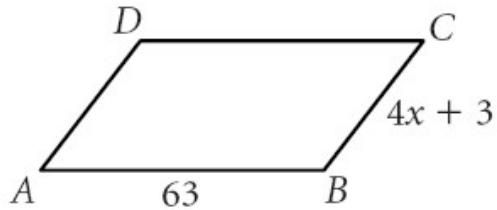
$$x = 35.5 \quad \text{**This means both sides } AB \text{ and } DC \text{ have a measure of } 35.5$$

$$AB = 35.5$$

Example 6: Find the missing measures in the parallelogram.

$$\text{Perimeter } ABCD = 16x - 12$$

$$AD = \underline{\hspace{2cm}}$$



Opposite sides of a parallelogram are congruent. We can add up the four sides and set that equal to the perimeter.

$$2(63) + 2(4x + 3) = 16x - 12$$

$$126 + 8x + 6 = 16x - 12$$

$$132 + 8x = 16x - 12$$

$$\quad -8x \quad -8x$$

$$132 = 8x - 12$$

$$+12 \quad +12$$

$$144 = 8x$$

$$\bar{8} \quad \bar{8}$$

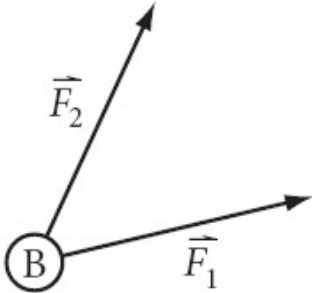
$$18 = x$$

$$AD = 4x + 3 = 4(18) + 3 = 72 + 3 = 75$$

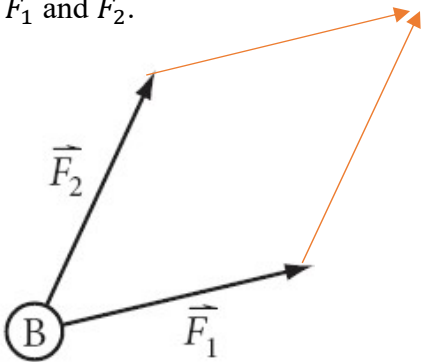
$$\mathbf{AD = 75}$$

Example 7: Complete.

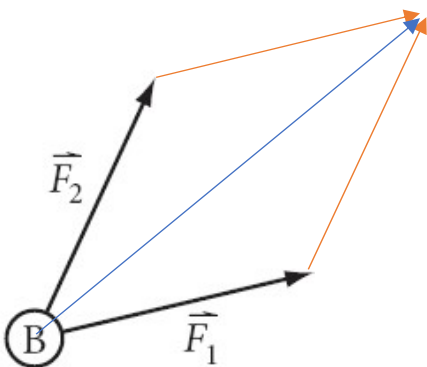
Ball B is struck at the same instant by two forces, \vec{F}_1 and \vec{F}_2 . Show the resultant force on the ball.



In order to find the resultant vector, we need to create a parallelogram using vectors equivalent to \vec{F}_1 and \vec{F}_2 .



The diagonal of the parallelogram is the resultant vector. So, we need to draw that in.



The blue arrow shows the resultant force on the ball.